DEVELOPMENT OF CORRELATIONS FOR THERMOPHYSICAL PROPERTIES OF SUBCRITICAL NITROGEN (SCN2) TO BE USED IN HIGH TEMPERATURE SUPERCONDUCTING (HTS) CABLES

DISSERTATION

IN PARTIAL FULFILLMENT OF THE REQUIREMENT FOR THE

AWARD OF THE DEGREE

OF

MASTER OF TECHNOLOGY

IN

MECHANICAL ENGINEERING

BY

AJAY KUMAR RAMANI

REG. NO: 11007370

UNDER THE GUIDANCE OF

MR. RAJA SEKHAR DONDAPATI

&

MR. GAURAV VYAS

DEPARTMENT OF MECHANICAL ENGINEERING

LOVELY PROFESSIONAL UNIVERSITY

PHAGWARA, PUNJAB, INDIA 144411

(May 2015)

LOVELY PROFESSIONAL UNIVERSITY, PUNJAB

CERTIFICATE

I hereby certify that the work which is being presented in the Dissertation entitled "**Development of Correlations for Thermophysical Properties of Subcritical Nitrogen (SCN2) to be used in High Temperature Superconducting (HTS) Cables**" in partial fulfillment of the requirements for the award of degree of **Master of Technology** and submitted in the Department of Mechanical Engineering, Lovely Professional University, Punjab is an authentic record of our own work carried during period of dissertation under the supervision of **Mr. Raja Sekhar Dondapati, Asst. Professor**, Department of Mechanical Engineering, Lovely Professional University, Punjab.

The matter presented in this dissertation has not been submitted by me anywhere for the award of any other degree or to any other institute.

Date: Ajay Kumar Ramani Reg. No: 11007370

This is to certify that the above statement mentioned by the candidate is correct to best of my knowledge.

Date: Mr. Raja Sekhar Dondapati (Asst. Professor and Supervisor) Lovely Professional University

The M.Tech Dissertation examination of **Development of Correlation for Thermophysical Properties of Subcritical Nitrogen (SCN2) to be used in High Temperature Superconducting (HTS) Cables** has been held on

Signature of the Examiner

DECLARATION

I, student of **Master of Technology (Thermal Engineering)** under Department of **Mechanical Engineering** of Lovely Professional University, Punjab, hereby declare that all the information furnished in this dissertation 1 report is based on my own intensive research and is genuine. This dissertation 1 does to the best of my knowledge, contain part of my work which has been submitted for the award of my degree either of this university without proper citation.

AJAY KUMAR RAMANI Registration No. 11007370

Date:

ACKNOWLEDGEMENT

First and the foremost I offer my sincerest gratitude to my supervisors, **Mr. Rajasekhar Dondapati**, Assistant Professor, School of Mechanical Engineering, Lovely Professional University, Punjab, **Mrs. Preeti Rao Usurumarti** who has supported me throughout my thesis with their patience, knowledge, valuable advice, uninterrupted active supervision and constant encouragement. I attribute the level of my Master's degree to their encouragement and effort without them this thesis, too, would not have been completed or written.

I express my heartfelt gratitude to **Dr. Loviraj Gupta,** Executive Dean **LPU and Dr. Amit Kumar**, Dean of the Department of Mechanical Engineering, **Dr. Gurpreet Singh Phull**, Head of the Dept. of Mechanical Engineering. and **Dr. Vijay Shankar,** Head of the School of M.E. and **Mr. Minesh Vohra,** Coordinator of M.E. Dept. Lovely Professional University, Phagwara for providing me the permission and necessary facilities in the department and giving me an opportunity to carry out my studies and thesis work effectively at the University

It has also been great opportunity for me to work under the support of **Mr. Gaurav Vyas**, Assistant Professor, School of Mechanical Engineering, Lovely Professional University, Punjab.

I am thankful to **Mr. Abhinav Kumar**, Assistant Professor, Mechanical Engineering, St. Soldier group of institutions, Punjab who continuously motivated, clearing concepts and encouraged me to do this research work.

I thank **Mr. Varun Goyel, Mr. Vishnu** and **Mr. Sarthak** for hearing my presentation regarding the progress of my work and providing me with the knowledge of valuable key points on which I must work on.

I would like to thank the faculty of School of Mechanical Engineering, Lovely professional University for attending my presentations regarding my research work.

I also grateful and needful to my **research group** for their encouragement and support in this research work.

I would again like to thank **Lovely Professional University** for giving me opportunity to use their resource and work in such a challenging environment. I am grateful to the individuals whom contributed their valuable time towards my thesis.

Last but not the least, I express my sincere gratitude to my parents, family members and all the friends who have always supported me throughout all my studies at university and encouraged me with their best wishes.

TABLE OF CONTENTS

LIST OF FIGURES

Figure 20: Breakage of density value at the boiling point due to phage change……………30 **Figure 21:** Density as a function of temperature at a pressure 23.958bar ………….…….…31 **Figure 22:** Polynomial curve fitting of Density data at a pressure 23.958 bar…….…...........31 **Figure 23:** Viscosity as a function of temperature at a pressure 23.958bar …………….…..32 **Figure 24:** Polynomial curve fitting of Viscosity data at a pressure 23.958 bar………….....32 **Figure 25:** Thermal Conductivity as a function of temperature at a pressure 23.958bar…....33 Figure 26: Polynomial curve fitting of Thermal Conductivity at a pressure 23.958 bar…....33 **Figure 27:** Specific Heat as a function of temperature at a pressure 23.958bar…………….34 **Figure 28:** Polynomial curve fitting of Specific Heat data at a pressure 23.958 bar………..34 **Figure 29:** Comparison of Correlation Fitted values v/s NIST values with Temperature .…38 **Figure 30:** Relative Errors of Correlation Fitted values with Temperature …………….…..38 **Figure 31: (a)** Geometry of CSP (b) Boundary Conditions (c) Meshed Structure of CSP....39 **Figure 32**: (a) Temperature Distribution (b) Heat Transfer (c) Flow Velocity Analysis40 **Figure 33(a):** Cooling Capacity v/s Temperature Difference for various flow rates41 **Figure 33(b):** Cooling Capacity with varying fluid Temperature and Flow Rates……….…41

LIST OF TABLES

ABSTRACT

The storage and transmission of energy have been a major challenge and objective over a past decade. To accomplish such an objective of improving the effectiveness of power transmission system, superconductivity principle is introduced in 1978 which has become a revolutionary step towards the new era of sustainable energy. The present electrical transmission systems suffer 40-60% transmission losses such as AC losses, thermal losses due to the use of conventional conductors. Therefore, in order to reduce these losses to minimum extent, most of the power transmission systems are to be replaced by High Temperature Superconducting (HTS) cables in power applications. Since the losses are dissipated in the form of heat, the need arises to choose a suitable coolant (cryogen) which can accommodate the heating load in view of development of room temperature superconductor.

 In present project work an attempt has been made to propose a novel cryogenic cooling concept with Subcritical Nitrogen $(SCN₂)$ to maintain superconducting state over a wide range of applications and hence minimize the transmission load. As the nitrogen is the major constituent in the atmospheric air, the concern over its availability may not arise. Thereby, it can be separated from air and can be converted in to $SCN₂$ using various cryocoolers. This report discusses the thermo-physical properties such as **density, viscosity, thermal conductivity and specific heat** of SCN₂. The **supercritical temperature and pressure** of nitrogen is obtained from NIST web book [10] as 126.19K (-146.81 ⁰C) and 3.3958MPa (33.958 bar) respectively, whereas **triple point** temp. is $63.15K$ (-209.85 ⁰C) and **normal boiling point** temp. is 77.355K (-195.645⁰C). It was found that near the critical point there is significant variation and superposition in the thermo-physical properties of $SCN₂$ with respect to temperature and pressure due to phase change and unit compressibility factor $(Z^{\dagger}1)$ and hence almost ideal gas behaviour is shown by $SCN₂$ cryogenic fluid.

 Further work of this dissertation is focussed towards the development of correlations for above thermo-physical properties, error analysis and compression of obtained results, reason for drastic variations and superposition of properties and identify the suitable range of working temperatures, which can be beneficial for predicting performance of cryogenics and thermo-hydraulic modelling of HTS cables in future and hence time and money can be saved by this mathematical modelling and simulation without manufacturing the actual prototypes. In recent times, with the sophistication and advancement of computer technology, solving of various transport equations with temperature dependent thermo-physical properties became easy and simpler. Hence this dissertation thesis and developed correlations would benefit the technological community and upcoming generations to develop futuristic smart power grid with HTS cables, a move toward the green world by replacing Conventional Cables.

KEYWORDS: Superconductivity, cryogenics, critical point, subcritical nitrogen, HTS.

NOMENCLATURE

T^c Critical Temperature

DEVELOPMENT OF CORRELATIONS FOR THERMO-PHYSICAL PROPERTIES OF SUBCRITICAL NITROGEN (SCN2) TO BE USED IN FUTURISTIC HTS CABLES FOR EFFICIENT POWER APPLICATIONS

CHAPTER 1

INTRODUCTION

1.1 RESEARCH NEEDS: PRESENT ENERGY SCENARIO

Energy is the driving source of all the phenomena of this physical world and it is the capacity of doing any work, so its proper management and utilization is a prime focus of study. Conservation of energy states that energy neither be created nor be destroyed, i.e. energy of the universe is conserved. As we in our daily life transforming the energy from one form to another form as per our requirements. So we need such an effective system to maximize the usage of energy to a greater extent. The total energy production of the world from all the sources is **13634 Million tonnes of oil equivalent (1Mtoe=11.63TWh)**, out of which **23132 TWh** is the share of electrical energy whereas the present electricity demand is too high as **29550 TWh** as per Enerdata 2014 **[48].** So to fulfil the required demand of electricity we need to optimize the whole systems/devices of energy generation, storage, transmission, distribution and utilization of conventional techniques which is only possible by replacing the normal conventional conductors and devices by High Temperature Superconducting (HTS) cables and systems. Since the existing power transmission system encountered up to 60% losses of energy from the generation point to the utilization point due to various types of losses in between i.e. AC losses, Thermal losses, Hysteresis losses, Magnetic losses, etc. However, energy production is more at the generation point but we get less than the half of that energy at the utility point. As shown in the below clustered column bar diagram the demand is very high and production is low and hence the consumption is low as per production amount. Due to the urbanization, industrialization and higher living standard of people the consumption and demand of electricity is

1

continuously increasing from the last decade and hence it is necessary to increase the production as well to fulfil the present need of electricity to the world.

 Figure 1 : Comparison of world's demand, production and consumption of electricity [48]

The top ten energy producer countries are shown in the below pie **chart (1)** in which China is the major producer contributes 30% of the total which India is in 5th rank shares 6% energy. These 10 countries share is 8781Mtoe to the total world energy production 13634Mtoe which is 64.4% **[50].** The transmission and distribution losses are shown in **figures 2 (a) and (b).**

Figures 2:(a)Top ten energy producer of world (b)Percentage T&D Losses worldwide [50]

1.2 BACKGROUND CONCEPTS AND AREA OF STUDY

The study of superconductivity at cryogenic temperatures comes under the field of **condensed matter physics**, so the brief concept must be understood prior to the study of superconductivity and the role of cryogens. Condensed matter physics is a broad category of physics that deals with the physical properties of condensed phases (states) of matter. **Solid and liquid** are the most familiar condensed phases, while more unusual and exciting condensed phases are the **superconducting phase** exhibited by certain materials and fluids at low temperature, the ferromagnetic and anti-ferromagnetic phases are found in cold atomic systems as spins of atomic lattices[1].

 In present era the study of **phase transitions** and **critical phenomena** is an focused and important part of modern science of condensed matter physics. Phase transition stands for the change of phase of a system and matter, which is brought about by change in an external parameter such as temperature, pressure etc. However quantum phase transitions refer to transitions of phase where the temperature is maintained at zero. The study of phase transitions and critical phenomena in correlated systems is an active area of research **[47].**

 Figure 3: Illustration of different phases with phase diagrams [51]

When the temperature of substance approaches critical temperature, the properties of its gas and liquid phases converge, resulting into only one phase at and beyond the critical point. This homogeneous and non-distinguishable phase is of fluid is known as supercritical fluid. The **heat of vaporization is zero** at and beyond this critical point, and so no distinction exists between the two phases. On the P-T diagram, the point at which critical temperature and critical pressure meet is **called the critical point** and **critical phenomena** of the substance. For pure substances, there is an inflection point in the critical isotherm (constant temperature line) on a PV diagram, Mathematically it means that at the critical point derivatives are zero.

$$
\left(\frac{\partial P}{\partial V}\right)_T = \left(\frac{\partial^2 P}{\partial V^2}\right)_T = 0
$$

Therefore the first and second partial derivatives of the pressure p with respect to the volume V at a constant temperature T are both zero at the critical point. It can be used for calculation of two parameters for an equation of state of substance in terms of the critical properties.

1.3 SUPERCONDUCTIVITY

Superconductivity refers to a phenomenon of exactly zero electrical resistance and exclusion or absence of magnetic fields occurring in certain materials and it alloys when cooled below a characteristic critical temperature (T_c). This phenomenon was discovered by **Dutch physicist Heike Kamerlingh Onnes on April 8, 1911** in Leiden for Solid Mercury (Hg) at **Tc of 4.2K** using liquid He. Superconductivity is a quantum mechanical phenomenon like Ferromagnetism.

Figure 4: Comparison of decrease in resistivity for Normal and Superconductor [49, 55,56]

1.3.1 Meissner Effect and Magnetic Levitations

Superconductivity is characterized by the Meissner effect, the complete exclusion or ejection of magnetic field lines from the interior of the superconductor as it enters or transitions into the superconducting state. The Meissner effect and its occurrence indicate that superconductivity can levitate a magnet i.e. it describe the absence of magnetic field within the superconductor. The working of MagLev trans based on this principle due to the repulsion of magnetic field.

Figure 5: Meissner effect for Superconductor compared with normal conductors [53]

1.3.2 Cooper Pairs and BCS Theory

John Bardeen, Leon Cooper, and John Robert Schrieffer ("BCS") in 1957 first proposed the microscopic theory of superconductivity, which is based on the zero bnd gap and the Condensatoion of Cooper Pairs into a boson-like state without violating the **Pauli exclusion principle.** However the energy gap is highest at low temperatures but the band gap vanishes at the transition temperature when superconductivity exist at the critical temperature. When the Cooper pair is passing through a conductor, it attracts the lattice, causing distortion and a slight ripple toward its path which causes the electron to get attracted to that displacement. The coupling between electrons is depicted in a Feynman diagram as below:

Figure 6: Illustration of cooper pairs and BCS theory [54]

1.4 MOTIVATION FOR THE REASEARCH

As the superconductivity is the phenomenon of zero resistivity of conductors at very low temperature i.e. at cryogenic temperature. So the application of superconductivity is impossible without cryogens such as Nitrogen, Hydrogen, Helium, Oxygen, Argon etc.. Thus the study of cryogenic is the prime field of research along with superconductivity and related applications such as HTS Cables, transformers, generators , SMES etc.

 Presently there is a wide application of cryogens in liquid state and in subcritical regions due to the various benefits and suitability of these fluid rather than the supercritical fluids. Many of research groups and organizations are currently involved in the research of cryogenic fluid in supercritical region and subcritical region also but the study of fluids in subcritical region has following pros over supercritical fluids:

- **a.** At a pressure and temperature below the critical point the handling of subcritical fluid is easy and safer than the supercritical fluid.
- **b.** The latent heat of vaporization of the fluid is max at the boiling point.
- **c.** The work required to pump and pressurized the subcritical fluid is lower.
- **d.** Specific vol. is low so required smaller storage tank than supercritical fluid.
- **e.** Subcritical fluid can be liquefied at high pressure whereas supercritical fluid can't be liquefied at any pressure and hence possess very high specific volume.

There are many types of gasses used as cryogenic fluids according to their range of temperature and pressure, stability of their thermophysical properties, and ease of availability. Here this research is confined in only the study of thermophysical properties of Nitrogen in the subcritical region i.e. Subcritical Nitrogen $(SCN₂)$ due to the following beneficial facts:

- a) Nitrogen is the most abundant gas, 78% of the air, so better availability at low cost.
- b) It is non-toxic, non-flammable, non-explosive, chemically stable and ease of handling.
- c) Large gap between saturation and critical temperature (50K), so more ref. effect (RE).

1.5 PROPOSED WORK AND ITS SIGNIFICANCE

The concept of superconductivity and the cryogenics (coolant) at supercritical and subcritical regions have been became more wide area of research application and thus gained much attention by researchers and engineers. As near critical point (sub critical region) and above critical point (supercritical region) at extreme pressure conditions the repulsive forces become important enough to overcome the surface tension and create almost single homogeneous phase which shares the properties of liquid and gases. At the critical point the isothermal compressibility of the one phase fluid becomes infinite **[4].** In the subcritical and transcritical regime, the thermophysical properties have non – linear relationship between the temperature and pressure. As the diffusivity and isobaric specific heat of cryogenics and supercritical fluid is high , it is considered as a proper solvent and coolant in many engineering applications**[2-3].**

 As we increasing the temperature of any fluid from beyond its **triple point**(where all phase boundary exist) to its **critical point** (where no phase boundary exist) the transition of phase occurs and get converted into the supercritical fluid.

The below diagram shows the **subcritical region** for water, which can be defined for other fluids also such as Nitrogen, Argon, Hydrogen, Oxygen etc. between the normal boiling point to the characteristics critical point. For Nitrogen it lies from temperature range of 77.355 K to its Critical point 126.19 K

Figure 7 (a), (b): Illustration of Subcritical and Subcritical region with phase diagrams [52, 10]

Critical phenomena and the formation of supercritical fluid of a substance is the result of dynamic phase equilibrium. When a material or fluid is heated until its specific critical temperature in a closed system (at constant pressure), a dynamic phase equilibrium is exist. This equilibrium state indicates that the same numbers of molecules coming out of the liquid phase to the gas by gaining energy and going into liquid phase from gas by losing energy. At this point, the phase curve between liquid and gas phases disappears and supercritical, a homogeneous phase appears. The **critical point** is **characteristic** of each material.

1.5.1 Application of Superconductivity and Function of Cryogens

Although the concept of superconductivity principle in engineering application is very useful in term of minimum energy losses and maximize the output in power generation, storage, transmission and distribution, but the major challenge is to achieve and maintain that extremely low temperature superconductivity phenomenon, which may exist within the temperature range of **-50 to -250 ⁰C** for different fluids like Helium, Hydrogen, Oxygen, Nitrogen etc. So the need of proper coolant arises to dissipate the heat losses for efficient operation of HTS Systems.

 The major function of any cryogen or coolant is to extract the heat from the superconducting device and maintain the cooling/refrigeration effect to achieve the desired temperature so that the operating condition can be kept stable and effective. Therefore the deep study and thermo-physical property analysis of cryogen with varying temperature and pressure is of major concern. Thus the development of correlations for major thermophysical and transport properties like thermal conductivity, specific heat, density, viscosity etc. would be very helpful for predicting the behaviour and performance of cryogen prior to actual application with the help of mathematical modelling and simulations. Liquid nitrogen cooling systems have been developed for HTS power devices over the past several years since liquid nitrogen is a cheap and excellent cooling medium and also a good electrical insulator. In recent research sub-cooled and subcritical Nitrogen are considered as important coolants. Compared to Supercritical and Saturated N_2 , SCN_2 could obtain higher efficiency and performance.

CHAPTER 2 TERMINOLOGY

2.1 CONDUCTORS AND SUPERCONDUCTORS

Normal conductors are the material which having properties of transferring free electrons and having less energy gap and forbidden gap between conduction band and valance band, but due to the random motion and high entropy of the moving electron there is collision among the metal ions and electron which causes losses. However in Superconductors at very low or critical temperature there is very less entropy and therefore electron are aligned as a cooper pairs and moves freely without collision with positive ions and hence no resistance is offered by conductors resulting zero losses and heat generations.

Types of Superconductors: (A) Type I Superconductor and **(B)** Type II Superconductor

Type I Superconductor: It consist generally soft superconductors, in which magnetization loss occurs suddenly and exhibit Meissner effect. These are made of Pb, Hg, Sn etc.

Type II Superconductors: Hard superconductors with gradual magnetization losses and does not exhibit meissner effect. These types are made up of Nb-Ti, Nb-Sn and their alloys. On the basis of Temperature Superconductors are further classified into two categories:

1. Low temperature superconductors $(T_c \leq 20K)$. [Here 77.35 K is the **Critical Point**]

2. High temperature superconductors $(T_c > 77K)$ [of N₂ which is taken as reference point]

2.2 CRYOGENICS AND CRYOGENIC FLUID

Cryogenic is the part of Physics and Engineering which deals with the production of very low temperature i.e. below -150⁰C or 123K and the study of material behaviour at this temperature.

H.K. Onnes in 1911 identified the zero resistance/ superconductivity of solid mercury at cryogenic temperature using Liquid Helium as refrigerant at **4.2 K**. There are various fluids which are used as refrigerant like Nitrogen, Argon, Hydrogen, Oxygen etc. for cooling.

CHAPTER 3 LITERATURE REVIEW

3.1 PRESENT RESEARCHES

This chapter includes the studies of various scientist and research scholars in the field of cryogenics and its application in superconductivity especially in HTS power transmission cables. As the this thesis is focussed to study the major thermophysical properties of nitrogen is subcritical region near the critical point and hence develop the simpler correlations as a function of temperature and pressure to predict the behaviour, stability and performance of nitrogen as a suitable cryogenics, thus review of literature is also done with reference to properties of nitrogen in a wide range of temperature and pressure i.e. triple point to critical point including saturation or boiling point.

3.2 STUDIES BY RESEARCHERS AND CO-WORKERS

 Richard T Jacobsen et al. (1973): They studied and tabulated the thermodynamic properties of Nitrogen in wide range of temperature and pressure including liquid and vapour phases from 63K(freezing line) to 2000K with pressures 0 to 10,000 Bar. Their property table include values of density, internal energy, enthalpy, entropy, latent heat, isochoric specific heat(C_V), isobaric specific heat (C_P), velocity of sound, the isotherm derivative $(\partial P/\partial \rho)T$ and isochoric derivative $(\partial P/\partial T)\rho$. The thermodynamic tables which they presented are based of on an equation of state $P = P(\rho, T)$ which represent liquid and gaseous nitrogen in above mentioned temperatures and pressures. An extensive comparison is carried out for estimated data calculated from equation of states with reference to experimental thermodynamic data of each property. The coefficients of the equation of states were determined by a weighted least squares fit to selected $P - \rho - T$ and other property to illustrate the agreement between calculated and experimental data with an uncertainty of $\pm 1\%$ [1].

- **Azad Jarrahian et al. (2012):** They suggested a novel correlation approach to estimate the thermal conductivity of pure carbon dioxide in the supercritical region. Their work for development of correlation to predict the performance of $SCCO₂$ created a curiosity to study the properties of cryogenic fluid below the critical point i.e. in subcritical region. Their study was mainly concerned about the correlation for thermal conductivity with the arithmetic average of the absolute value of relative errors(AARE) as 32.12% and sum of absolute of residual (SAR) as 5239 which is better than the prediction of *Bahadori and Vuthaluru* **[5]***.*
- **Ali Akbar Amooey (2014):** He also recently proposed a simple thermal conductivity correlation as a function of density and temperature for $SC\text{-}CO₂$ taking 600 data points. After statistical calculation, validation and comparison of results he concluded that the proposed correlation has better performance with lower AARE%(2.74) and SAR value(1044), hence having higher prediction abilities at a wider range of temperature from 290 K to 800 K and density from 1 to 1200 kg/m^3 with respect to **Jarrahian et al. and Bahadori et al**. Models **[6]**

3.3 STUDIES ON VARIOUS TYPES OF LOSSES

3.3.1 AC Losses in Conductors

When the AC current is varied the magnetic field would certainly leads to the movement of distraction which causes the induced e.m.f & current in the normal region as a result loss occurs due to this heat is being dissipated in the superconductor. This is known as AC losses in the HTS. AC losses in HTS conductors comprise of hysteresis losses due to self or external fields, eddy losses due to currents in sheath materials and coupling losses due to the presence of multiple filaments in HTS tape $[11]$. So in order to dissipate heat loads $SCN₂$ may plays a vital role due to its unique thermophysical properties.

R.Wesche et al., [1999] studied "Design of Superconducting cables" investigations shows [11]: Losses in superconducting cables are mainly due to AC losses, Thermal losses and

dielectric losses. Cable geometry, operating conditions, transmitting power and resulting losses. According to Wesche, Bi-2223 cables with warm dielectric are operating well below 77 K. Temperature, 45-50 K, Bi-2212 super-conductors could be a best alternative instead Bi-2223. Properties of Superconductors for various cable applications.

- **J.A.Demko et al., [2001]** studied "Practical AC Loss and Thermal Considerations for HTS Power Transmission Cable Systems" investigations are as follows **[12]:** Counteracting ac losses and thermal losses by using parallel flow and counteracting flow arrangements, in both the arrangements, high temperatures are reached in the cable at lower flow rates (1000 g/s). In counter flow, the system temperature, at which the LN_2 is returned to refrigerator, is lower than the cable maximum. In parallel flow, it is quite opposite. Finally increasing the flow reduces the maximum temperature at the expenses of higher pressure drop.
- **◆ H.Noji [2003]** studied "AC losses analysis of 114 MVA high-T_c superconducting model cable" investigation shows **[13]:** By using Electric circuit (EC) method the AC losses analysis for single phase HTS cable has been found out. Comparing axial field (B_{am}) and circumferential field (B_{cm}) , B_{cm} values are dominant in the applied fields. Moreover, B_{cm} in the electrical shielding is low compared with B_{cm} in the conductor. This tendency strongly influences the distribution of the layer losses in the conductor. In the electrical shielding, the layer losses consist of W_{self} and W_{BC}
- **M.Yagi et al., [2003**] studied "Measurement of AC Losses of Superconducting Cable by Calorimetric Method and Development of HTS Conductor with Low AC Losses" investigations are as follows **[14]**: AC losses of 1 W/m level at 3 kArms obtained by enhancing winding pitches and twisted filaments in the tape. Accuracy of AC losses in a 3 m HTS conductor was 0.09 W/m with a measurement distance 2 m and flow rate of 0.5 kg/min. Placing insulation breaks between inner pipe and outer pipe eliminated the induced loss and the eddy current losses.

- \div **H.Noji et al., [2005**] studied "Numerical analysis of the AC loss in a high-T_C superconducting cable measured by calorimetric method". His investigations shows [15]: Calculated AC losses on HTS cable manufactured by Furukawa Electric Industries Ltd (FEI) by using Electric Circuit method. Measured AC losses on HTS cable (FEI) by using Calorimetric method. The measured AC losses and Calculated AC losses show almost equal. Layer's current are uniform on the low transport current. This indicates the driftcurrent phenomenon at higher transport current region.
- **K.Ryu et al., [2010]** studied "AC losses of the 5 m BSCCO cables with shield" investigations are as follows [16]: To measure the AC losses for multi-layered conductor and shield of HTS cable of 22.9KV/50MVA. Analysed results show that, AC loss measured from the lead attached to the shield (shield-lead) is constant irrespective of I_t . But the measured loss from the lead attached to the conductor is greatly dependent on transport period. Thick insulation around the conductor leads to exertion of heat transfer by the coolant around the conductor. As I_t high, the conductor temperature rises and thus the AC loss measured from the conductor-lead increases 1.5 times larger than that from the shield-lead.
- **Vysotsky et al.,[2011]** studied "AC losses and other researches with 5 m HTS model cable" investigations are as follows **[17]:** This test facility has taken place in Russian scientific R&D institute to perform extensive tests of heavily instrumented HTS cable model up to 5 m. Various test includes, critical current measurement, current distribution measurement among layers and joint resistance etc. For 5 m HTS cable models of 1G and 2G tapes, AC losses test has discussed.

3.3.2 Fluid and Pressure Losses

These losses are due to the variation in density and viscosity of the cryogenic fluid as the operating temperature and pressure of the cryogenic fluid rises therefore the intermolecular distance between the atoms will be less thereby the variation in transport properties leads to

pressure drop and Heat transfer inside the HTS cable. So in order to overcome such challenges, SCN can be used due to viable transport properties at operating temperatures and pressures.

- **Posada. A et al., [2006]** studied "On conduction-cooling of a high-temperature superconducting cable" investigations are as follows **[21]:** Design of HTS cable with a copper layer incorporated in its thermal insulation, can achieve conduction cooling of HTS tape below its T_c . Various provisions considered for doing analysis, cable lengths, widths and insulation/copper thickness. Cable cost is minimised because there is no pumping requirement of cryogenic fluids.
- **J.A. Demko et al., [2009**] studied "Cooling configuration Design considerations for Long Length HTS Cables" His investigations are as includes **[20]**: HTS cable configurations were studied with a numerical model to asses thermal hydraulic performance with AC and thermal losses. Performance of long length cable systems for normal operating and fault conditions in a counter flow cooling geometry is perceived. Counter flow cooled, long length, HTS cables are technically feasible, energy saving and lower cost and it requires less cryostat. Analysed results, for 1000 meter HTS cable system it is feasible to build these lengths and stable recovery to full operating current can be achieved in reasonable.
- **Rajasekhar Dondapati and V.V. Rao [2013]** studied "Pressure drop and Heat transfer analysis of Long length internally cooled HTS cable". Their investigations show **[23]:** Analysis reveals, the phenomenon of turbulence preferment and heat transfer in HTS cables. At constant corrugation depth, pressure drop and Heat transfer increase with increase in corrugation pitch. To achieve efficient heat transfer, twisted tapes is inserted into the coolant path, elevating turbulence. Thermo physical properties of LN2are considered to be temperature dependent. Pressure drop and heat transfer carried out for different flow rates of LN2.At constant corrugation depth, the pressure drop increases with increases in corrugation pitch. In order to increase heat transfer twisted tapes are inserted by creating turbulence.

 \triangle **A.Sasaki et al., [2011]** studied "LN₂ circulation in cryopipes of superconducting power transmission line" His investigations includes **[22]:** Different kinds of losses in SC PT's some are from coolant circulations others from radiation penetration into the cryopipe. Losses are directly proportional to the cable length, are large compared to the conduction loss through the current leads in the long distance systems.

3.3.3 Dielectric Losses in HTS Cable

Dielectric losses occur between the high temperature superconductor and shield material. In a cable with warm dielectric, each phase requires a separate high voltage cryostat enclosed in a conventional dielectric. The main disadvantage of this concept is the magnetic interaction of the different phases and eddy current losses. Whereas cold dielectric, it is immersed in **LN²** and conductors are in direct contact with the coolant..

- **J.A.Demko et al., [2003]** studied "Cryostat Vacuum thermal considerations for HTS Power Transmission Cable Systems" investigation are as follows **[19].** Effects of degraded vacuum levels on the operation of HTS cables for different cryogenic thermal insulation systems have been studied. Two basic cable configurations being demonstrated are 1. Warm-dielectric (WD) 2. Cold dielectric (CD) and this study is based on single phase HTS cable for different lengths (100m and 1000m). CD cable shows, slightly higher temperature because there are ac losses in both the main and shield layers, which are at LN_2 temperatures. In both the cases, the pressure drops are not very high and do not change significantly due to extra heat loads caused by the degraded vacuum. Pressure drop over the 100m section is less than 0.9 bar for WD cable and less than 0.1 bar for CD cable.
- **J.A.Demko et al., [2005]** studied "Testing of the dependence of the number of layers on the performance of a one meter HTS Transmission Cable section" investigations are as follows [**20**]. Measurement of the dc V-I characteristics and the ac loss have been made on southwire company cable in the original four layer configuration and by

varying with different layers (three, two and one layer cable). Different measurements used for finding ac loss measurements are calorimetric and electric method were used for one layer cable to within a factor of two. Electrical method, higher sensitivity at lower currents and the sample preparation is much simpler than the calorimetric method. The measured data for the four layer and one layer cable were compared against calculations using both the Monoblock model and Dresner model. When Ip/Ic \leq 1 then ac loss is closer for four layer cable. For one layer cable both model is Ip/Ic \leq 1. The HTS cable had a long response time for smaller current increase over some stable operating limit.

- \div **T. Nakatsuka¹ et al., (2014) [26]:** Research and develop the basic technology of HTS cable, fault current limiter, and transformer. Also study the 3 kA superconducting cable, cooling technology of HTS cable length 500m and power system analysis of cable and AC equipment's. The basic technologies have been started for the design of HTS cable by testing works. The feasibility studies for HTS cable also have been studied by power system analysis.
- **Dong Zhang¹et al., (2012) [27**]**:**5 m/10 kA HTS DC power cable was developed which helps to investigate the design of a conductor, fabrication, current carrying capacity and stability of the 360 m/10 kA HTS power cable. A 5 m/10 kA HTS DC power cable has been designed, fabricated and tested to evaluate the performance of the 360 m/10 kA HTS DC power cable, which connect the rectifier output of a substation with the bus bar of an electrolytic aluminum cell in Henan Zhongfu Industrial.
- **Francesco Grilli ¹ et al., (2012)** [**28**]**:** Evaluated the ac losses of HTS tapes and wires as well as of assemblies such as cables and coils. The formulation, used in the magnetic field components as state variables, had proved an efficient implementation to solve 2- D problems, which involves infinitely long or axially-symmetric geometries. Successfully implemented a 3-D model for time-dependent Simulations of high-

temperature superconductors using the H-formulation. The model has been validated by comparing the results with cases that can be solved in 2-D and has been used to show different examples of application on 3-D geometries.

- **Marijn Oomen¹ et al., (2012)** [**29**]**:** Investigate the use of 2nd-generation High-Temperature Superconductors (2G-HTSs) in the rotors of electrical motors and generators. It is operated in vacuum at temperatures around 30 K, in strong magnetic fields of about 2T.Impregnated Coils are desirable. Several of the coils show degradation of the superconducting properties. Three large impregnated 2G-HTS racetrack coils with kA current capacity were produced and successfully tested. Mechanical properties of 2G-HTS, their uniformity and fatigue behavior are studied.
- **Schmidt¹ et al.,(2009)** [**30**]**:** The integration of a high voltage cable in a networks always a particular case and in field of superconducting cables several designs are already available to fulfill the technical and environmental requirements. Superconducting cables have significant benefits for power transmission and distribution applications that provide new aspects and possibilities in network planning.
- **S.C. Kim¹ et al., (2007)** [**31**]**:** Two different Ag round wires are considered with different Ag ratio were fabricated by using powder in tube method and processing factor at each step was investigated. Microstructure after pre-annealing was investigated. Drawing stresses of two wires at first and second bundle wire are almost the same. In order to evaluate the uniformity of filaments, investigated COV of the wires.
- **Tosin Famakinwa¹ et al., (2007)** [**32**]**:** The eddy current losses in the matrix of two twisted filaments Bi-2223 HTS tapes in applied external AC magnetic field was calculated using 3D FEM software. Numerical calculation results shows that the Contribution of eddy current loss at commercial frequency is not minimum. The numerical results presented are for uncoupled filaments HTS tapes.

- **T. Hemmia¹ et al., (2006) [33**]**:** Study the current decay behaviors in HTS coils using Bi-2223/Ag tapes. Demonstrate that the resistance is enhanced due to the decay of the shielding current by the flux creep and flux flow. Results are compared with numerical analysis using a FEM. Current decay behavior is also discussed by choosing an overshooting excitation technique. The current decay behaviors are found to be affected by shielding currents. Improvement in decay behaviors is possible using appropriate excitation process like overshooting the initial current. It is determined by the joint resistance.
- **H.J.Kim¹et al., (2004)** [**34**]**:** This paper is based on the study of electrical insulation properties of dielectric paper, such as breakdown voltage, partial discharge, which is one of the HTS cable structure elements. The PPLP had a high tensile stress in liquid nitrogen, but low tensile strain. As tensile stress increased the breakdown stress of PPLP was decreased because of micro crack occurrence.
- **Mitsuho Furuse¹ et al., (2003) [35**]**:** Establishment of long distance cooling techniques and design of a compact cross section are required for development of HTS cables. Temperature distributions of counter flow cooled HTS power cable and designed 3 different cable structures. These are effective from the view point of cooling design to produce compact cables**.**
- **ShinchiMukoyama¹ et al., (2003) [14]:** Reducing losses in large capacity cables and cooling cables. Obtain design data and improve the production technologies for the manufacture and installation of 500m cable.
- **Chikashi Suzuki¹ et al., (2003)** [**36**]**:** In this paper an investigation is done on the optimal design for the cabling parameters, Crossections of pitch length, dimensions of tape for YBCO and former diameter. Transverse bending strain can be calculated with the cabling parameters longitudinal bending strain can also be calculated.

- **Takato Masuda¹ et al., (2002)** [**37**]**:** Developed a 3-core 66 kV class HTSC cable and shield wound with Ag–Mn sheathed Bi-2223 tapes, insulation with polypropylene laminated paper impregnated with liquid nitrogen and thermal insulation with Co-axial corrugated pipes. The results of these tests clarifies good performance of the cable such as critical current value 2.4 kA, AC loss with 0.5 W/m/phase at 1 kA and AC 130 kV withstand voltage. It has the basic electric properties required to a 66 kV HTSC cable.
- **Yanhua Yang et al., [2009],** in their research paper "A new heat transfer correlation for supercritical fluids" **[45]** have indicated that: The heat transfer of supercritical fluids shows abnormal behavior as compared to that of conventional fluid. The new correlation can be applied to both normal and Heat Transfer Deterioration (HTD) conditions. New correlation shows better results as compared to the earlier developed correlations.
- **Z.Q. Long et al., [2013],** in their research "Natural convective heat transfer of supercritical helium in a closed vertical cylinder" **[46]** have indicated that The natural convective heat transfer of supercritical helium in a closed vertical cylinder gives excellent heat transfer performance as compared with that of conventional gases. Heat transfer can be enhanced by increasing the helium charging amount. In the Rayleigh number range (5 X 1010 to 2 X 1014), the Nusselt number increases almost exponentially with the Rayleigh number 9.
- **Raja Sekhar Dondapati and V.V. Rao [2014],** in their research paper "Entropy generation minimization (EGM) to optimise mass flow rate in dual channel cable-inconduit conductors (CICCs) used in fusion grade magnets" **[24]** have indicated that: Factors that affect entropy generation in CICC include heat transfer, flow with friction and mixing of flow streams. Optimum mass flow rate was calculated at which heat transfer rate is highest. In dual channel CICC, entropy generation due to thermal

gradient dominates as compared to that of velocity gradient. In his work, optimum rate of entropy generation as found as a function of mass flow rate.

- **Anbin Chen et al., [2010],** in their paper "Design of the cryogenic system for a 400kW expertal HTS synchronous motor**" [38]** have indicated that the designed model has the heat load of 730.4 W. This heat load is the sum of heat leaks from the surroundings and internal heat generation in the device. By taking the basis of heat load, cryogenic system was designed.
- **S.K. Baik et al., [2006],** in their paper "Effect of synchronous reactance and power factor on HTS synchronous machine design and performance" and "Electrical Design of a 17MW Class HTS Motor for Ship Propulsion" **[43-44]** have concluded that as synchronous reactance becomes smaller, it is possible to get better design results and performance characteristics at steady state condition. Moreover, smaller synchronous reactance increases armature current at transient states such as fault condition and motor starting.
- **Minseok Joo et al., [2004],** in his paper "Dynamic control of large scale high temperatures uperconducting synchronous motor" **[41**] has indicated that the control strategy of starting the high temperature superconducting synchronous motor with constant field windings is to give gating signal commands during accelerating period.
- **Sang-Ho Lee et al., [2008],** in their paper "Study on homopolar superconductivity synchronous motors for ship propulsion applications" **[42]** have analysed for superconducting synchronous motors and their applications in ship propulsion application with effective cooling

CHAPTER 4 RATIONALE AND SCOPE OF STUDY

4.1 OBJECTIVES OF THE STUDY

As discussed and investigated in previous chapters and literature reviews it will be very helpful and beneficial to study the performance and behaviour of cryogenic fluids to be used in superconductivity applications. Thus the development of correlation for thermophysical properties of fluid will be an effective ways to predict the performance. Therefore the main objective of this research can be summarized as follows:

- \triangleright To analyse and identify the major thermophysical properties of nitrogen which plays major role in its application as a cryogenic at very low temperature and high pressure.
- \triangleright To study phase diagram of Nitrogen in subcritical region and draw the conclusion.
- \triangleright To study the temperature dependent variation and the nature of trends of the two major thermophysical properties, i.e. thermal conductivity and isobaric specific heat and two major transport properties i.e. density and viscosity of Nitrogen in the subcritical region.
- \triangleright To develop and proposed a novel temperature dependent correlation for a wide range of temperature, so that the study of its performance as a cryogenic will be easier in future.

4.2 SCOPE OF THE STUDY

The major role of cryogenic in superconductivity and HTS cables is to extract the heat, which is dissipated as a result various losses such as thermal losses, AC losses, etc. So it is necessary to analyse the heat transfer nature and thermophysical properties more precisely at a less interval of temperature. During its application in underground HTS cable the fluid has to be pumped and circulated within the steel corrugated pipe carrying the cable. So it is also necessary to study the flow behaviour and transport properties of Nitrogen in the subcritical region, which will be helpful in pressure drop analysis, frictional loss calculation and pumping power calculation for different length and current carrying load of HTS cable.

CHAPTER 5 RESEARCH METHODOLOGY

5.1INTRODUCTION

Redman and Mory define research as a "systematized effort to gain new knowledge or in other words it is art of scientific investigation. To carry any research and study the research methodology is the heart of analysis and study. This is very crucial stage of study which requires lots of attention and investigation on the research problem. It includes the step by step progression of research toward the results. It is an iterative process in which lots of iteration is required to refine the results and reach to the expected outcomes. The research methodology will be shown as the below flowchart:

Figure 8: Flow chart for the research methodology

5.2 USE OF MATHEMATICAL TOOL

The present research is based on quantitative approach and data analysis to develop the temperature dependent correlation for each of the four major properties of Nitrogen. The formulation of research problem is to propose the correlation for thermophysical properties in the subcritical region. All the data are extracted from the **NIST web book** for the wide range of temperature and pressure in subcritical region of Nitrogen. After graphical investigation and data analysis it was found that there is drastic variation of property values in the specified sub critical region so it will be complicated to develop a single correlation for the whole data in subcritical region. Therefore multiple range of temperature was be taken and hence the multiple correlation will be develop as a piecewise continuity of polynomial functions. This required a number of iteration and investigation. The suitable range of temperature was identified for different pressures. After that **Linear Regression and Correlation Techniques** will be employed to develop the correlations and for minimizing the errors **Least Square Method** will be used. The linear regression model is defined as follow:

In this research study the dependent variable are all of the four properties and temperature is the independent property, i.e. the resultant correlation will be temperature dependent.

5.3 STUDY OF MAJOR PROPERTIES OF NITROGEN

Temperatures (K)	Thermal	Specific Heat	Density	Viscosity
At $P=1.03215$ bar	$Cond.(W/m-K)$	$(KJ/kg-K)$	(Kg/m3)	$(Pa-s)$
Near TP 63.251	0.17726	1.9999	866.96	3.07E-04
AT BP 77.355	0.14581	2.0415	806.08	$1.61E-04$
ATBP 77.355	0.0075	1.1239	4.6121	$0.0544E-04$
Near CP 126.15	0.01241	1.0547	2.7334	0.0864E-04

Table 1: Values of Major Thermophysical Properties of Nitrogen at Specific Points [25]

Table 2: Various Cryogenic Fluids and their normal characteristics points [25]

Cryogen	Triple Point [K]	Boiling Point [K]	Critical Point [K]
Methane	90.7	111.6	190.6
Oxygen	54.4	90.2	154.6
Argon	83.8	87.3	150.9
Nitrogen	63.1	77.3	126.2
Neon	24.6	27.1	44.4
Hydrogen	13.8	20.4	33.2
Helium	2.2	4.2	5.2

After going through the extensive literature review on various issues related to study of thermophyscal properties of cryogenic fluids and their application in cooling of HTS Cables, it is found that there is research gap i.e. no work is done for major properties of $SCN₂$ as cryogens. So major four properties i.e. Specific Heat, Thermal Conductivity, Density and Viscosity are chosen, which play vital role in heat transfer and flow circulation for cooling of HTS Cables. Here table (2) shows various cryogenic fluids out of which this dissertation describe only about Nitrogen in Subcritical region as a better cryogenic refrigerant for cooling of HTS cable at wide range of pressures and temperatures.

5.4 STUDY OF MAJOR THERMOPHYSISCAL PROPERTIES OF SCN²

DENSITY: It is defined as the mass of fluid per unit its volume, i.e. it specify that how closely the molecules are packed in the fluid, closer the packing means they are denser. The SI unit of density is $kg/m³$ and denoted as ρ . The density of Nitrogen is high in liquid state in the temperature range between TP to BP. Whereas it drastically reduced after the boiling point as the phase changes from liquid to vapour phase. As shown in table at BP temperature density is 806.08 kg/m³ in liquid state and 4.6121 kg/m³ in vapour state. So it is preferable to in the temperature range above BP to Critical point. Lesser dense fluid will need lesser pumping power and hence circulation of cryogenic will be easier in the HTS cable.

Figure 9: Density of Subcritical Nitrogen as function of temperature and pressure [10]

Figure 10: Density as a function of temperature at different pressures [10]

VSCOSITY: It is the major factor responsible for flow behaviour and pressure drop of cryogenic fluid within the corrugated steel pipe carrying the HTS cable. It is defined as the resistance offer by any fluid during its flow due to shear stress between the different layers of fluid. Its SI unit is pa-s and denoted as μ and kinematic viscosity as v. As shown in table the viscosity of Nitrogen is very less of the order 10^{-4} in liquid as well as in vapour state. It is also decreasing as the temperature rises due to increase in internal energy. At BP the values of viscosity is **1.61E-04 pa-s** and **0.0544E-04** pa-s respectively in liquid and vapour states, i.e. in vapour state viscosity is reduced by approximately by 30 times.

Figure 11: Viscosity of subcritical Nitrogen as function of temperature and pressure [10]

Figure 12: Viscosity as a function of temperature at different pressures [10]

> **THERMAL CONDUCTIVITY:** It is major thermophysical property of cryogenic fluid in the heat transfer point of view, as it shows the property of material to conduct the heat and it is evaluated by using Fourier's law of heat conduction. It is often denoted as k, λ , or κ and its SI unit is W/mK. High thermal conductivity materials are used in heat sink or cooling application and low thermal conductivity material are used in thermal insulation application. At boiling point due to the phase change from liquid to vapour all the properties have two different values, one for liquid phase and other for vapour phase. The K values at boiling point are 0.14581 and 0.0075 respectively. It can be seen that as the temperature approaches to critical point K value decreases.

Figure 13: Thermal Conductivity of SCN² as function of temperature and pressure [10]

Figure 14: Thermal Conductivity as a function of temperature at different pressures [10]

ISOBARIC SPECIFIC HEAT: It is defined as the amount of heat required for the temperature of unit mass of fluid by $1⁰C$ at constant pressure. Its SI unit is KJ/kg-K and denoted as C_{P} . Since it signifies the required heat energy, so for ideal refrigerant low specific heat is desirable. As shown is table the specific heat of Nitrogen is less and continuously decreasing after BP and near critical point, it is minimized (1.054KJ/kg-K

Figure 15: Specific Heat of SCN² as function of temperature and pressure [10]

Figure 16: Specific Heat as a function of temperature at different pressures [10]

5.4.1 Conclusion for Thermophysical Properties

Thus after analysing all the above major properties of Nitrogen it can be concluded that it is suitable for cryogenic cooling of HTS cables and can minimize all losses during its application.

Figure 17: All the prop. as a function of temperature at a pressure 23.958bar [10]

Here in the above figure (17), variations of all the four properties are well compared within the range 77.355K – 126.15K. There is increase in thermal conductivity whereas specific heat and viscosity are almost constant with temperature. The increase in thermal conductivity and decrease in density value are desirable for cryogenic refrigerant point of view, as less dense fluid will need lesser pumping power and higher thermal conductivity will favour the rapid heat transfer rates, whereas constant viscosity may offer less viscous loss and pressure drop.

Figure 18: Properties of N² compared with other cryogens at their Critical Pressure [10]

Here Nitrogen is compared with Oxygen, Argon and Hydrogen at their critical pressure as shown **figure (18).** The higher values of thermal conductivity and specific heat whereas lower values of density and viscosity shows dominating applicability of Nitrogen over other cryogens

CHAPTER 6

RESULTS AND DISCUSSION

6.1 STUDY OF PHASE DIAGRAM AND PHASE CHANGE

The trends of extracted data from the NIST web book for thermophysical property of Nitrogen in subcritical region shows the drastic variation and with rise in temperature at a particular pressure. So after data analysis it is found that at a pressure of 23.958 bar the thermophysical properties shows continuous variation within he temperature range 77.355 K to 119.00 K and then from 119.15 K to 126.15 K. This breakage of range is due to the fact that 119.07 K is the boiling point of Nitrogen at a pressure of 23.958 bar and hence phase change occurs. Thus at that particular point of temperature all the properties have two different values, one for liquid phase and another vapour phase. For example it can be seen for density of Nitrogen as below:

Figure 19: Temperature- density and P-V diagram of Subcritical Nitrogen [25]

 Figure 20: Breakage of density value at the boiling point due to phase change [10]

6.2 POLYNOMIAL CURVE FITTING AND DEVELOPMENT OF CORRELATIONS

The outcome of this research is the temperature dependent correlations for thermophysical properties of Nitrogen in the subcritical region for different suitable range of temperature. The correlation are obtained by using the mathematical curve fitting technique using **Linear Regression Model** and **Least Square Method**. The curve fitting is polynomial as per trends of variation of data and extent of errors with respect to exact fit. Since exact fit is very rare due presence of residual errors so best fit is desirable to obtain the simple correlation. In exact curve fitting the curve passes through each data points whereas the best fitted curve only concern those major points which follow a particular trend and variation.

6.2.1 Curve Fitting for Density Data

 Figure 21: Density as a function of temperature at a pressure 23.958bar [10]

Figure 22: Polynomial curve fitting of Density data at a pressure 23.958bar [10]

6.2.2 Curve Fitting for Viscosity Data

Figure 23: Viscosity as a function of temperature at a pressure 23.958bar [10]

Figure 24: Polynomial curve fitting of Viscosity data at a pressure 23.958bar [10]

6.2.3 Curve Fitting for Thermal Conductivity Data

Figure 25: Thermal Cond. as a function of temperature at a pressure 23.958bar [10]

Figure 26: Polynomial curve fitting of Viscosity data at a pressure 23.958bar [10]

Here the figure () shows almost linear variation of thermal conductivity with respect to temperature (77.355K-119.15K) which follows first order linear equation $y = mx + c$, whose slope (m) is **– 0.00196** with positive X-axis and intercept on Y-axis (c) is **0.29929.**

6.2.4 Curve Fitting of Isobaric Specific Heat Data

Figure 27: Specific Heat as a function of temperature at a pressure 23.958bar [10]

Figure 28: Polynomial curve fitting of Specific Heat data at a pressure 23.958bar [10]

After the best curve fitting of all the data for Density, Dynamic Viscosity, Thermal Conductivity and Isobaric Specific Heat for suitable temperature ranges got the simple polynomial temperature dependent correlations which is well tabulated and described in section - 6.2.5 with their polynomial coefficients and correlation coefficients.

6.2.5 FINALLY DEVELOPED TEMPERATURE DEPENDENT CORRELATIONS

Table 3: Correlation Table for all the properties of SCN2 for different T ranges

M 35

M

6.3 STATISTICAL PARAMETERS FOR VALIDATION OF CORRELATIONS

There are various statistical parameters for the validation and error analysis of obtained results. All those parameters will be employed at the final stage of research to assure the accuracy and suitability of research results. In order to ascertain the quality of the proposed fitted model and correlations, statistical following parameters will be used. Small values of parameters refer to dependable correlation.

 The Arithmetic Average of the Absolute Values of the Relative Errors **(AARE%)** is defined as

defined as
\n
$$
AARE\% = \frac{100}{N} \sum_{i=1}^{N} \left(\left| \frac{X_i^{\exp} - X_i^{\text{cal}}}{X_i^{\exp}} \right| \right) \dots \dots \dots \text{41}
$$

 \triangleright It is an indication of the accuracy of the correlation. Another parameter is defined as Sum of Absolute of Residual (SAR) which is defined below shows the reliability of correlation for more dense data points.

 …………. {2} exp 1 *N cal i i i SAR X X*

 \triangleright The Average Percent Relative Error (ARE%), which is defined in Eq. (3) gives a measure of the bias of the correlation, a value of zero indicates a random of the measured values around the correlation.

$$
ARE\% = \frac{100}{N} \sum_{i=1}^{N} \left(\frac{X_i^{\exp} - X_i^{\ cal}}{X_i^{\exp}} \right) \dots \dots \dots \dots \tag{3}
$$

 The **Percent Relative Error (RE%)** which is defined in Eq. (4) Measures the calculated values w.r.to experimental values. for each thermophysical properties correlation as a function of temperature.

$$
RE\% = 100 \times \left(\frac{X_i^{\exp} - X_i^{\text{cal}}}{X_i^{\exp}}\right) \qquad (4)
$$

 The **Adj. R-Square Value(Curve Fitting Coeff.),** which is defined in Eq.(5) gives the degree of approximation of curve fitted w.r.to exact curve fitting for equations.

$$
R^{2} = 1 - \frac{\sum_{i=1}^{N} (X_{i}^{\exp} - X_{i}^{\text{cal}})^{2}}{\sum_{i=1}^{N} (X^{\text{mean}} - X_{i}^{\text{cal}})^{2}}
$$
............(5)

Table 4: Values of Statistical Parameters for fitted curves and correlations

PROPERTIES	TEMP.	AARE%	ARE%	SAR	$\overline{\mathbf{R}^2}$
DENSITY	TR1 TR ₂	0.688326	6.88E-01	1912.7869	0.9996
		4.719823	$4.71E + 00$	325.39993	0.9999
	TR1 TR ₂	3.152771	3.15772	59.13E-05	1.0000
VISCOSITY	TR ₃	0.574809	1.00E-02	9.600E-05	0.9993
		$3.601E + 01$	$3.61E + 01$	25.429E-05	0.9992
SPECIFIC	TR ₁ TR ₂	$2.161E + 01$	$2.16E + 01$	221.4477	0.9929
HEAT		1.599942	9.96E-02	3.157411	0.9992
THERMAL COND.	TR ₁ TR ₂	0.2679530	0.1285998	0.104779	0.9998
		1.1797511	$1.18E + 00$	15.635E-03	0.9963

6.4 ERROR ANALYSIS OF DEVELOPED CORRELATIONS

As discussed in above **section 6.3**, these parameters are very helpful to justify the fitted values of correlations with the experimental NIST values. Here all the four temperature dependent properties are plotted taking into account their relative errors with respect to the values of NIST web book. Minimum error shows correlations are not much biased.

Figure 29: Comparison of Correlation Fitted v/s NIST values with Temperature [10]

Figure 30: Relative errors of Correlation Fitted values with Temperature [10]

As shown in **figure 30** the relative errors are much lesser and closer to zero line. The errors lie within a narrow range of $+0.3$ to -0.9 , which indicates the dependency and reliability of the developed correlation. The errors may be due to the less precision in taking the interval of analysis. Moreover these errors can minimized to greater extent by taking fine temperature intervals and more number of iterations during the data analysis and interpolation of values.

6.5 EXTENDED FUTURE WORK

This research work can be further extended for Design and Simulation work using the developed correlation function for various major properties of Subcritical Nitrogen $(SCN₂)$. Heat transfer and Flow analysis are of major concern to judge the better suitability and applicability of Nitrogen cryogenic fluid as a refrigerant for better cooling of HTS cables. Therefore a prototype of corrugated steel pipe **(CSP)** of internal **diameter 40mm and 3m of length [23]** is taken for simulation in **COMSOL** Multiphysics Software. For heat transfer analysis 2D **convection and conduction mode** and for flow velocity analysis the **incompressible Navier-Stokes equation** mode is applied. The results are shown below:

6.5.1 Heat Transfer and Flow Velocity Analysis

(c)

Figure 31: (a) Geometry of CSP (b) Boundary Conditions (c) Meshed Structure [57]

After solving the simulation problem with applied boundary conditions and subdomain settings, following results are observed:

- \triangleright There is a uniform and minimum temperature distribution on the surface of former.
- \triangleright The inlet temperature is 63K and rises to 126K when exiting out by absorbing heat.
- \triangleright Heat transfer rate and temperature rise is more along the center of the corrugated pipe.
- \triangleright Heat absorbed by subcritical Nitrogen circulating along center is around 7.543KW.
- \triangleright There is minimum velocity and better circulation of Nitrogen cryogen near the wall.
- \triangleright Corrugated geometry of wall surface provides better turbulence of fluid and flexibility.
- \triangleright Flow velocity is maximum about 1.55 m/s along the center of the corrugated steel pipe.

Figure 32: (a) Temp. Distribution (b) Heat Transfer (c) Flow Velocity Analysis [57]

6.5.2 Cooling Capacity for Different Volume Flow Rates

The main purpose of cryogenic fluid is to cool the HTS cables by dissipating the heat and maintaining the superconducting state during the entire application of transmission. Therefore analysis and study of cooling capacities for different flow rates are of prime concern for better heat dissipation and effective transmission of current in HTS cable. Here cooling capacities at different flow rates and fluid temperatures are analyzed at **23.958bar** and a fixed wall temperature of **164K**. It can be seen from the **figures 33 (a) and (b)** that as the temperature difference and volume flow rates increase form **5L/min to 10L/min** the cooling capacity get increased accordingly from 14.44KW to 28.95KW. Although the increased flow rates may cause more pressure drop within the pipe and also require more pumping power to circulate it continuously, however it will be more effective and preferable for stationary cooling application such as for transformer etc.

Effective and preferable for stationary cooling application such as for transformer etc.
 $\text{cooling } _\text{Capacity} = \rho^* V^* C_p^* (T_w - T_f) _\text{maximum}$ (6)

Figure 33(a): Cooling capacity v/s temp. difference for various flow rates[10]

Figure 33(b): Cooling capacity with varying fluid temperature and flow rates[10]

CHAPTER 7 CONCLUSIONS AND FUTURE SCOPE

After proper analysis of all the major thermophysical properties of Nitrogen in the subcritical region from triple point to critical point it is found that subcritical fluid has better performance as a cryogenic. At a pressure and temperature below the critical point, the handling of subcritical fluid is easy and safer than the supercritical fluid. The latent heat of vaporization of the fluid is maximum at the boiling point. The work required to pumping the subcritical fluid is lower. Specific vol. is low so required smaller storage tank than supercritical fluid. Subcritical fluid can be liquefied at high pressure whereas supercritical fluid can't be liquefied at any pressure and hence there may be storage problem due to very high specific volume.

 The developed Correlations will not need big computations & large number of parameters. Lower AARE%, ARE% and SAR and Adj. R-Square values very close to 1 identify will give a better and dependable approach for prior analysis of Subcritical Nitrogen in the application for cooling of HTS Systems & Cables. A Convenient and Suitable subcritical temperature regime $(77.355K-119.15K)$ of $SCN₂$ has been identified which can be used in Futuristic HTS Cables and their cooling applications for efficient power transmission. Therefore the above correlations tabulated at table (3) may be beneficial and convenient for the prior analysis and simulations of Subcritical Nitrogen before using it as a cryogenic fluid.

 The further study of this research is can be extended to develop more realistic and accurate correlations with minimum errors or without errors.The development of futuristic HTS cable with better utility and practical applications by employing new cooling concepts. Subcritical fluids have better scope in cryogenics so similar investigation can be done for other fluids like Helium, Argon Oxygen etc. Moreover this work can also play a crucial and major role for designing; modelling and simulation of various HTS analysis as a reference such as Flow Velocity, Pressure drop and Heat transfer Analysis etc. using developed correlations.

CHAPTER 8

LIST OF REFERENCES

- [1]Richard T Jacobsen and Richard B. Stewart, "Thermodynamic Properties of Nitrogen Including Liquid and Vapour Phases from 63 K to 2000 K with Pressures to 10,000 Bar ", J. Phys. Chem. Ref. Data, Vol. 2, No. 4 (1973).
- [2]Erdogan Kiran, Pablo G.Debenedetti and Cor J.Peters, " Supercritical Fluids: Fundamental and Applications", Series E: Applied Sciences-Vol. 366.
- [3]Erdogen Kiran, Johana M.H. Levelt Sengers, "Seprcritical Fluids Fundamentals for Application", NATO ASI Series, Vol.273(1993).
- [4]J.P. Hickey, M.Ihme, "Supercritical mixing and Combustion in Rocket Propulsion", Center for Turbulence Research, Internal Report, Annual research Briefs,(2013).
- [5]Azad Jarrahian, Ehsan Heidaryah, "A novel correlation approach to estimate thermal conductivity of pure carbon dioxide in the supercritical region", J. of Supercritical Fluids 64 (2012): 39–45.
- [6]Ali Akbar Amooey," A simple correlation to predict thermal conductivity of supercritical carbon dioxide", J. of Supercritical Fluids 86 (2014)1–3.
- [7]Ehsan Heidaryan, Azad Jarrahian,"Modified Redlich–Kwong equation of state for supercritical carbon dioxide", J. of Supercritical Fluids 81 (2013): 92–98.
- [8]J.G.Weisend, John Barclay et al, "Advances in Cryogenic Engineering" Transactions of the Cryogenic Engineering Conference-CEC, Volume 57A (13-17 June 2011).
- [9]D.Beysens, J. Straub, D.J. Turner, "Phase Transitions and Near Critical Phenomena", H.U.Walter(ed), Fluid Sciences and Materials Science in Space © European Space Agency, Paris Cedex, France 1897.
- [10]OriginLab Corporation, "Scientific Graphing and Data Analysis Software" One Roundhouse Plaza, Suite 303 Northampton, MA 01060 USA, 2015.
- [11]R. Wesche, a Anghel, B. Jakob, G. Pasztor, R. Schindler, and G. Vécsey, "Design of superconducting power cables," *Cryogenics,* vol. 39, no. 9, pp. 767–775, Sep. 1999.
- [12]J. A. Demko, J. W. Lue, M. J. Gouge, J. P. Stovall, U. Sinha, and R. L. Hughey, "Practical AC Loss and Thermal Considerations for HTS Power Transmission Cable Systems," vol. I, no. 1, 2001.
- [13]H. Noji, K. Haji, and T. Hamada, "AC loss analysis of 114 MVA high-Tc superconducting model cable," *Phys. C Supercond.*, vol. 392–396, pp. 1134–1139, Oct. 2003.

- [14]M. Yagi, S. Tanaka, S. Mukoyama, M. Mimura, H. Kimura, S. Torii, S. Akita, and a. Kikuchi, "Measurement of ac losses of superconducting cable by calorimetric method and development of HTS conductor with low AC losses," *IEEE Trans. Appiled Supercond.*, vol. 13, no. 2, pp. 1902–1905, Jun. 2003
- [15]H. Noji, "Numerical analysis of the AC losses of 500-m HTS power cable in Super-ACE project," *Cryogenics (Guildf).*, vol. 47, no. 2, pp. 94–100, Feb. 2007.
- [16]K. Ryu, Y. H. Ma, Z. Y. Li, S. D. Hwang, and H. J. Song, "AC losses of the 5m BSCCO cables with shield," *Phys. C Supercond.*, vol. 470, no. 20, pp. 1606–1610, Nov. 2010.
- [17]V. S. Vysotsky, A. a. Nosov, S. S. Fetisov, and K. a. Shutov, "AC Loss and Other Researches with 5 m HTS Model Cables," *IEEE Trans. Appl. Supercond.*, vol. 21, no. 3, pp. 1001–1004, Jun. 2011.
- [18] L. H. T. S. Cables, J. A. Demko, and R. C. Duckworth, "Cooling Configuration Design Considerations for," vol. 19, no. 3, pp. 1752–1755, 2009.
- [19] J. A. Demko, J. W. Lue, M. J. Gouge, D. Lindsay, M. Roden, D. Willen, M. Daumling, J. E. Fesmire, and S. D. Augustynowicz, "Cryostat vacuum thermal considerations for HTS power transmission cable systems," *IEEE Trans. Appiled Supercond.*, vol. 13, no. 2, pp. 1930–1933, Jun. 2003.
- [20]J. A. Demko, J. W. Lue, R. C. Duckworth, M. A. Young, M. J. Gouge, D. Lindsay, J. Tolbert, M. Roden, D. Willén, and C. Træholt, "Testing of a 1 . 5-m Single-Phase Short-Sample Cable Made With Copper Laminated HTS Tapes at ORNL," vol. 15, no. 2, pp. 1755–1758, 2005.
- [21]A. Posada, Y. I. Kim, and V. Manousiouthakis, "On conduction-cooling of a hightemperature superconducting cable," *Cryogenics (Guildf).*, vol. 46, no. 6, pp. 458–467, Jun. 2006.
- [22]A. Sasaki, Y. Ivanov, and S. Yamaguchi, "LN2 circulation in cryopipes of superconducting power transmission line," *Cryogenics (Guildf).*, vol. 51, no. 9, pp. 471– 476, Sep. 2011.
- [23]R. S. Dondapati and V. V Rao, "Pressure Drop and Heat Transfer Analysis of Long Length Internally Cooled HTS Cables," *IEEE Appiled Supercond.*, vol. 23, p. 5, 2013.
- [24]Raja Sekhar Dondapati and V.V. Rao, "Entropy generation minimization (EGM) to optimize mass flow rate in dual channel cable-in-conduit conductors (CICCs) used for fusion grade magnets", J. of Fusion Engineering and Design, vol. 89, 2014
- [25]E.W. Lemmon, M.O. Mclinden, and M.L.Huber," NIST standard reference database physical and chemical properties division", version 7.0,beta,7/30/2002, USA.

- [26]T. Nakatsuka, A. Kikuchi, Y. Ozawa, and K. Ueda, "Research and development of superconducting cable in Super-ACE project," vol. 42, no. 2002, pp. 345–350, 2009.
- [27]D. Zhang, S. Dai, F. Zhang, T. Huang, Y. Wang, Y. Lin, Y. Teng, G. Zhang, L. Xiao, and L. Lin, "Design research on the conductor of 10kA class HTS DC power cable," *Cryogenics (Guildf).*, vol. 52, no. 12, pp. 725–729, Dec. 2012.
- [28]F. Grilli, R. Brambilla, F. Sirois, A. Stenvall, and S. Memiaghe, "Development of a three-dimensional finite-element model for high-temperature superconductors based on the H-formulation," *Cryogenics (Guildf).*, vol. 53, pp. 142–147, Jan. 2013.
- [29]M. Oomen, W. Herkert, D. Bayer, P. Kummeth, W. Nick, and T. Arndt, "Manufacturing and test of 2G-HTS coils for rotating machines: Challenges, conductor requirements, realization," *Phys. C Supercond.*, vol. 482, pp. 111–118, Nov. 2012.
- [30]F. Schmidt and A. Allais, "superconducting cables for power transmission applications – a review," pp. 232–237, 2008
- [31]S. C. Kim, D. W. Ha, S. S. Oh, I. Y. Han, C. E. Bruzek, J. G. Oh, and H. S. Sohn, "Study on thermo-mechanical treatment in fabrication of Bi2212/Ag HTS wire," *Cryogenics (Guildf).*, vol. 47, no. 7–8, pp. 437–441, Jul. 2007.
- [32] T. Famakinwa, Q. M. Chen, "3D finite element analysis of eddy current loss of HTS tapes – External field analysis," *Phys. C Supercond.*, vol. 459, pp. 18–23, Aug. 2007.
- [33]T. Hemmi, N. Yanagi, G. Bansal, K. Seo, K. Takahata, and T. Mito, "Electromagnetic behavior of HTS coils in persistent current operations," *Fusion Eng. Des.*, vol. 81, no. 20–22, pp. 2463–2466, Nov. 2006.
- [34]H. J. Kim, D. S. Kwag, Y. S. Kim, and S. H. Kim, "Electrical characteristics of high-Tc superconducting mini-model cable under mechanical stresses in liquid nitrogen," *Cryogenics (Guildf).*, vol. 45, no. 1, pp. 45–50, Jan. 2005.
- [35]M. Furuse et al., "Investigation of structure of superconducting power transmission cables with LN2 counter-flow cooling," *Phys. C S,cond.*,vol. 386, pp. 474–479, A2003.
- [36]C. Suzuki, K. Goto, T. Saitoh, and T. Nakatsuka, "Strain prop of transposed segment conductors for a transmission cable," *Phys. C Supercond.*, pp. 1186–1191, Oct. 2003.
- [37]T. Masuda, T. Kato, H. Yumura, M. Hirose, S. Isojima, S. Honjo, K. Matsuo, T. Mimura, and Y. Takahashi, "Experimental results of a 30 m, 3-core HTSC cable," *Phys. C Supercond.*, vol. 372–376, pp. 1555–1559, Aug. 2002.
- [38]Anbin Chen, Xiaoku, "Design of the Cryogenic System for a 400kW Experimental HTS Synchronous Motor", IEEE Transaction on Applied Superconductivity, June 2010
- [39]D Inácio, S Inácio, J Pina et al., "Nemerical and Experimental Comparison of electromechanical Properties and efficiency of HTS and Ferromagnetic Hysteresis Motors", 8th European Conference on Applied Superconductivity, 2007
- [40]Ion Dobrin, Alexandru M. Morega, Milhail Popescu, "The Development of a Small Power High Temperature Superconductor (HTS) Synchronous Motor", Annals of the Craiova, Electrical Engineering Series, No. 34, 2010.
- [41]Minseok Joo, "Dynamic Control of Large Scale high temperature superconducting synchronous motor", IEEE Transact. on applied superconductivity, vol. 14, no. 2, 2004
- [42]Sang-Ho Lee, Jung-Pyo Hong, Young-Kil Kwon, Young-Sik Jo and Seung-Kyu Baik,"Study on Homopolar Superconductivity Synchronous Motors for Ship Propulsion Application",IEEE Transaction on Applied Superconductivity, Vol.18, No.2, June 2008.
- [43]Sengkyu Baik, Youngkil Kwon, "Electrical Design of a 17MW Class HTS Motor fornShip Propulsion", J. Supercond, 2013
- [44]S.K. Baik, M.H. Sohn et al., "Effect of synchronous reactance and power factor on HTS synchronous machine design and performance", IEEE Trans on app. supercond., 2006.
- [45] Yanhua Yang, Xu Cheng, Shanfang Huang, "A new heat transfer correlation for supercritical fluids", Front. Energy Power Eng. China, 3(2):226-232, 2009
- [46] Z.Q. Long, P. Zhang, "Natural convection heat transfer of supercritical helium in a closed vertical cylinder", Journal of Cryogenics,Elsevier, 2013
- [47] Neeraj Khare, "Introduction to High temperature superconductors", Internal Report, National Physical Laboratory, New Delhi
- [48] Enerdata, "Global Energy statistical data book", 2014
- [49]Bob Emery "catholic education, physics, emery, from ideas to implementation", 2015.
- [50] Statistics and Data of International Energy Agency, USA, 2015.
- [51]"Revised Release on the IAPWS Industrial Formulation for the Thermodynamic Prop. of Water and Steam". Int. Association for the Properties of Water and Steam. 2007.
- [52]A. Haghighi Asl and M. Khajenoori, "Subcritical Water Extraction, Mass Transfer Advances in Sustainable Energy and Envt. Oriented Numerical Modeling" 2013.
- [53] Hoffman Lab Dept. of Physics, Harvard University, 17 Oxford Street, Cambridge.
- [54]Chad Orzel, "science blogs principles, how-do-superconductors-work", 2010/08/03.
- [55]Christopher J.Wells Technology"Physics-Electrical -Basic Electrical Theory 2.5.2015
- [56] Dwi Prananto, "BCS Theory,condensed matter physics, Phonon, physics, Superconductivity" May 6, 2012.
- [57]Stockholm and Sweden founder COMSOL Inc. COMSOL Multi physics Simulation software / FEA Software, 1986.

APPENDIX

THERMOPHYSICAL PROPERTIES OF SUBCRITICAL NITROGEN

